### How to use Instrumental Variables

Questions that can be answered with experiments:

**Questions that can't be answered with experiments:** 

h, o dh ppen oq n yde nded fi'r se pr ce  
e pe o her de er n n s of de nd he s, e Pr ce e s c y of de nd  
Foo h pr ce see effec on q n y de nded 
$$P \rightarrow Q$$
  
h, o dh ppen o re, GDP fi'r se re, n eres r e  
e pe o her de er n n s of re, GDP he s, e ope of c ree  
Foo h re, n eres r e see effec on re, GDP  $r \rightarrow Y$ 

# How you *can't* answer nonexperimental questions:

co ec d, here 
$$r$$
, es of n eres r gg e  
cross e e ser es  
n s cross sec on  
e n s p.ne  
nd o serre co ore en s e een  $r_{2}$ , es  
ec, se o her de er n n s.re  $r_{1}$  n cond ons e corre d h red en  
Any h ng h, ch nges one econo c  $r_{2}$ , e ch nges o hers oo gener eq r ?  
Remarse c, s, y  
inq n y de nded red en s P  
o her  $r_{2}$  es h, ffec  $Q^{D}$  perh ps corred en h P, o her P s  
is pp y Q P  
ind c me red en s r  
o her  $r_{2}$  es h, ffec Y perh ps corred en h r.G.Y e por s Y<sup>e</sup>  
is py or r e r = r + Y-Y + - \*

#### How to approach nonexperimental questions

```
gnore referse c_{z} s_{z} y_{z} and corre c_{z} on hoher de er n_{z} hoher de er hoher 
                             o d p pers
                            econo e r cs f e d here go z s o de ons r z e echn q e no z ns er q es ons
Ans erq es on for d ode no re d or d
                    in ode yo c ne ogeno s y r gg e r e of n eres

\mathbf{\overline{p}} of q n fy p r e ers s e ode s r e nd f red ced for s od zz
          N<sub>f</sub> r<sub>f</sub> e per en s
                      F nd so e r gg es n re en \mathbf{r}_{t} e h re ncorre ed h o her de er n n s
                      Of en nes es ns r en t et t e
                                      so e h ng e s re, e h, c, ses or nd c, es r gg es n re, en F, e re eF, n n corre, ed h o her de er n, n s F, d
eg nq n y de nded rac{}_{z} e h ffecss pp y no de nd
                    n c r e ogeno s r ons n cen r n se ng of r
```

# In terms of regressions

$$Y = X + {}_{2}X_{2} + = X +$$

$$X \text{ For eso e Fr}_{i} e X_{2} \text{ Con ro Fr}_{i} e X = n e s r_{i} e de er n n s$$

$$Gener_{i} eq r \text{ pro e s}_{i} X = X + X = X + X = X + X = X_{i} + X_{i} = 1 X_{i} + X_{i} = 1$$

### How do you find instruments? How do you know if possible instruments are *relevant* and *valid*?

Fin to hy X res Ls poss ere sons Fin to oher de er non s of Y Ls poss e X s h ch re sons for re on the net ed of and esr e

### Statistical methods to test whether candidate Z's are relevant, strong & valid

Loo 
$$\chi$$
 firs s ge regress on  
Chec s gn s gn f c n ce gn de p s e of coeff c en on Z  
Bec se of e nsr en pro e s s or F s s for p e Z s  
need o e os gger h n R e of h  $\chi$  e s  
Loo red ced for regress on of Y on Z  
 $Y = \begin{cases} Z + Z^2 + 1 \\ Z - Z^2 + Z^2 + 1 \end{cases} + 2X_2 + \frac{1}{2}$   
gn gn des of coeff c en s sho d e cons s en h s ory  
if yo h e ore h n one Z X s or er den f ed yo c n es one Z g ns o hers  
see f res s re cons s en chross Z s  
 $\chi$  d y e c s on res r c on e ns Z s n corre ed h Y - X -  $\frac{1}{2}X_2$   
 $\chi$  Ge es  $e^{-\frac{1}{2}x_1^2}$  is n corre ed h Y -  $\frac{1}{2}X_2$   
 $\chi$  fig n es for  $\frac{1}{2}L$  finsen es for GMM  
Z s re O f yo f o re ec hypo hes s

Are lagged Y

## Are lagged Y's and/or X's valid instruments? con

#### **Example: supply and demand**

Yo 
$$p = e^{-1} e^{-1}$$

#### **Bottom line for you**

ne⊫erye prc, nyhng For y o e e hy  $X \rightarrow r$  es cross o ser ons h n yo r s p e **Choose one fro** e o t do no t t o effects s n de nde s c y c resope  $\mathbf{F}_{t} e^{t \operatorname{geh}_{t}} \operatorname{os} \mathbf{F}_{t} \operatorname{on} \operatorname{n} X \operatorname{s} \operatorname{ncorre}_{t} \operatorname{ed} \operatorname{h} \operatorname{n} e^{s \operatorname{r}_{t}}_{t} \operatorname{ed} \operatorname{e} \operatorname{er} \operatorname{n}_{t} \operatorname{nsof} Y$ c se B f ed ode d se ns r en s l f yo choose d For  $e = h_z c_z \sec Z \operatorname{s} o \operatorname{resc}_z \operatorname{resc}_z \operatorname{resc}_z \operatorname{ed} \operatorname{h} X$  hy hey  $\operatorname{resc}_z \operatorname{resc}_z \operatorname{d} \operatorname{h} X$  hy hey  $\operatorname{resc}_z \operatorname{resc}_z \operatorname{d} \operatorname{h} X$ ho f rs s ge nd red ced for regress ons Prome Z s reno e hr e of h F es s or  $R^2$  s or o her es s  $\blacktriangleright$  n ess yo c n t e  $\blacktriangleright$  ery s rong pr or c se for  $\blacktriangleright$  d y sho t rg n or es